

## Artificial Neural Networks: Complex solutions or complex confusion?

### 1. Definitions

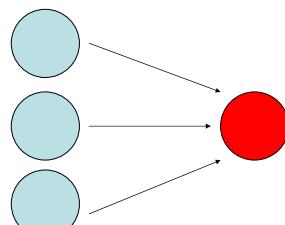
- Neural Network [1]-
  - "An interconnected assembly of simple processing elements, units or nodes, whose functionality is loosely based on the animal brain. The processing ability of the network is stored in the inter-unit connection strengths, or weights, obtained by a process of adaptation to, or learning from, a set of training patterns."
- Cost Function [2] – "
  - Given: a function  $f: A \rightarrow \mathbb{R}$  from some set  $A$  to the real numbers
  - Sought: an element  $x_0$  in  $A$  such that  $f(x_0) \leq f(x)$  for all  $x$  in  $A$  ("minimization") "

### 2. Structure

- Feedforward system
- Recurrent system
- Linearly Separable
- Non-linearly Separable
- Auto-associator
- Hidden Layer

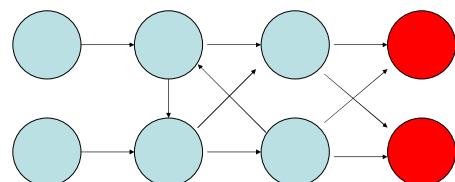
### 2. Structure: Feedforward

- Characterized by an acyclic graph that flows from input nodes to output nodes



### 2. Structure: Recurrent

- Represented by a cyclic graph, which allows for feedback loops



### 2. Structure: Linear

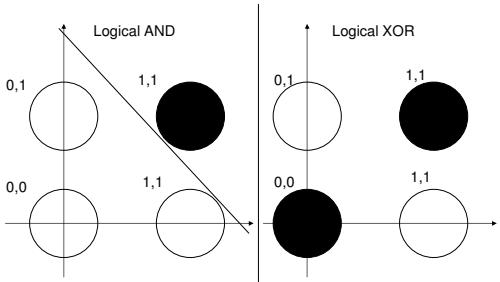
- The response function of a node is a linear combination of its inputs, like logical OR[3]

$$\begin{array}{c} \text{Inputs} \\ \swarrow \\ \begin{matrix} 0 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 1 \end{matrix} \\ \times \\ \begin{matrix} 1 \\ 1 \\ 0 \end{matrix} \\ = \\ \begin{matrix} 0 \\ 1 \\ 1 \\ 1 \end{matrix} \\ \searrow \text{Weights} \\ \text{Output} \end{array}$$

• Note: A seemingly nonlinear problem can often be rewritten as linear by adding inputs

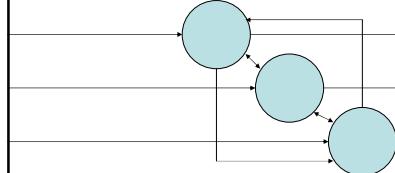
## 2. Structure: Non-linear

- Linearity refers to separation of solution space[3]



## 2. Structure: Non-linear

- A Hopfield network is a non-linear example [4]
- All of its nodes are symmetric without self loops.
- Each node has an energy associated with it.
- The network randomly turns nodes off and on to minimize the sum of all energy

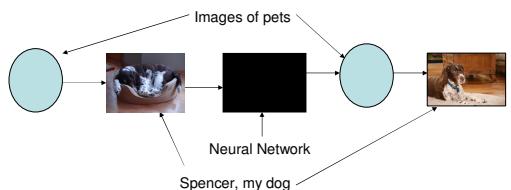


## 2. Structure: Non-linear

- In a Boltzmann machine, the amount of energy in a system affects the probability of whether a node is off or on. [5]
- As the network runs, the temperature decreases, and the process “anneals” or comes to a solution.

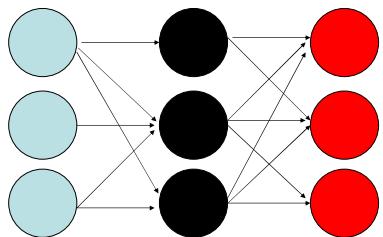
## 2. Structure: Auto-associator

- The prefix, auto, denotes self. Auto refers to input. The range of outputs is a subset of inputs. Basis of pattern recognition. [3]



## 2. Structure: Hidden Layer

- A hidden layer helps to minimize the error between the input and the responses



## 3. Learning Process

- Supervised Learning
- Unsupervised Learning
- Reinforcement
- Back-propagation

### 3. Learning Process: Supervised

- A series of inputs with known expected outputs are provided and the network attempts to minimize error.
  - Widrow-Hoff Learning for Linear Function
    - Initialize weights to 0
    - Until expected output matches network's output
      - Randomly select an input
      - Take cross product of weights with input
      - Calculate delta<sub>i</sub> for each w<sub>i</sub> where  $\text{delta}_i = w_i * (\text{correct output} - \text{actual output}) * \text{input}_i$
      - Add delta<sub>i</sub> to w<sub>i</sub>

### 3. Learning Process: Unsupervised

- The neural network is given a cost function that is some function of the input and the neural network's output
- The network's goal is to find an optimal, but, in practice, relatively minimized, cost function

### 3. Learning Process: Reinforcement

- Instead of waiting until the output is evaluated, the neural network is given feedback on its progress throughout its evaluation of the data
- This feedback allows the network to strengthen or weaken links between nodes

### 3. Learning Process: Back-propagation

- Back-propagation is an example of supervised learning where something like Widrow-Hoff is used at each layer to minimize the error between the layer's response and the actual data
- The error at each hidden layer is an average of the previously evaluated error
- Hidden layer networks are trained this way

### 4. Outlook

- Arguments for neural networks
  - Well suited for pattern recognition [6]
  - Can fly a plane [7]
  - Turing-complete

### 4. Outlook

- Arguments against neural networks
  - Requires intense computational power
  - Nigh on impossible to translate into a meaningful model
  - Machine learning often requires we know the answer to the problem

## References

- [1] "Neural Networks" *Proteome Society Glossary*. 2005. <http://www.inproteo.com/nwglosno.html>
- [2] "Optimization (mathematics)." *Wikipedia, The Free Encyclopedia*. 11 Mar 2008, 09:43 UTC. Wikimedia Foundation, Inc. <[http://en.wikipedia.org/w/index.php?title=Optimization\\_%28mathematics%29&oldid=197440261](http://en.wikipedia.org/w/index.php?title=Optimization_%28mathematics%29&oldid=197440261)>
- [3] Abdi, H. (1994). "A Neural Network Primer" *Journal of Biological Systems*.
- [4] "Hopfield net." *Wikipedia, The Free Encyclopedia*. 12 Feb 2008, 22:58 UTC. Wikimedia Foundation, Inc. <[http://en.wikipedia.org/w/index.php?title=Hopfield\\_net&oldid=191009263](http://en.wikipedia.org/w/index.php?title=Hopfield_net&oldid=191009263)>
- [5] "Boltzmann machine." *Wikipedia, The Free Encyclopedia*. 11 Mar 2008, 20:10 UTC. Wikimedia Foundation, Inc. <[http://en.wikipedia.org/w/index.php?title=Boltzmann\\_machine&oldid=197551222](http://en.wikipedia.org/w/index.php?title=Boltzmann_machine&oldid=197551222)>
- [6] Ness, Erik. "Artificial Networks fill in for taxonomists" *Conservation Magazine*. January-March 2005. Vol 6, No. 1 <http://www.conbio.org/cip/article61WEB.cfm>
- [7] "NASA Neural Network Project Passes Milestone" September 2, 2003. NASA Dryden Flight Research Center. <http://www.nasa.gov/centers/dryden/news/NewsReleases/2003/03-49.html>